## If the probability that a problem will be solved by three people is $1 / 2,1 / 3$ and $1 / 6$, then what is the probability that the problem will be solved?

If you find this type of problem to be difficult just draw a TREE diagram and it will put all your logic in place for many variants of the problem.



From this Probability Tree you can easily find such things as:

1. Probability $($ all 3 solve it $)=\frac{1}{2} \times \frac{1}{3} \times \frac{1}{6}$
2. Probability (only 1 solves it)
$=\mathrm{P}(\mathrm{A}$ solves, B not, C not $)+\mathrm{P}(\mathrm{A}$ not, B solves, C not $)+\mathrm{P}(\mathrm{A}$ not, B not, C solves $)$
$=\frac{1}{2} \times \frac{2}{3} \times \frac{5}{6}+\frac{1}{2} \times \frac{1}{3} \times \frac{5}{6} \quad+\frac{1}{2} \times \frac{2}{3} \times \frac{1}{6}$
3. Probability (none solve it) $=\underline{1} \times \underline{2} \times \underline{5}=\underline{5}$
$\begin{array}{llll}2 & 3 & 6 & 18\end{array}$
4. Probability (at least I person solves it)
$=$ the SUM of the top 7 outcomes on the list (a bit long - winded though!!)
A cleverer way is to realise all the probabilities must add up to $\mathbf{1}$
Probability (at least I person solves it) $=1-$ Probability (nobody solves it!)

$$
\begin{aligned}
& =1-\frac{5}{18} \\
& =\frac{13}{18}
\end{aligned}
$$

