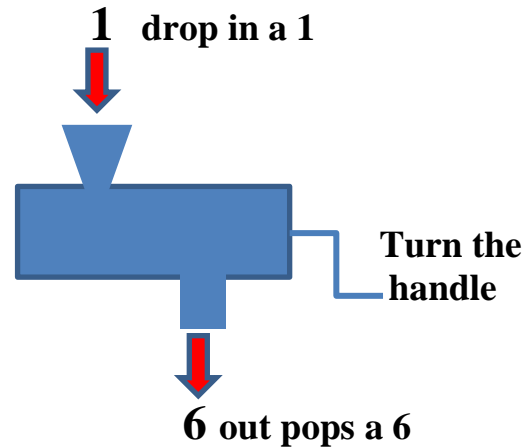


## What is an inverse function?

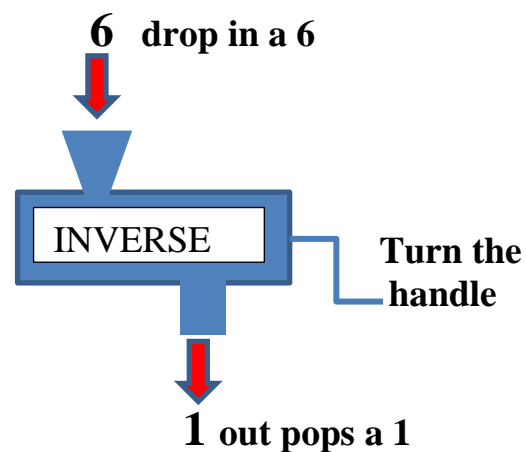
If you have an equation for example  $y = 2x + 4$  we can think of this as a formula for **changing x values into y values**.

For instance: If  $x = 1$  then  $y = 2 + 4 = 6$

Think of it as a machine like this...



An **INVERSE FUNCTION** would be an equation to **change 6 back into 1**

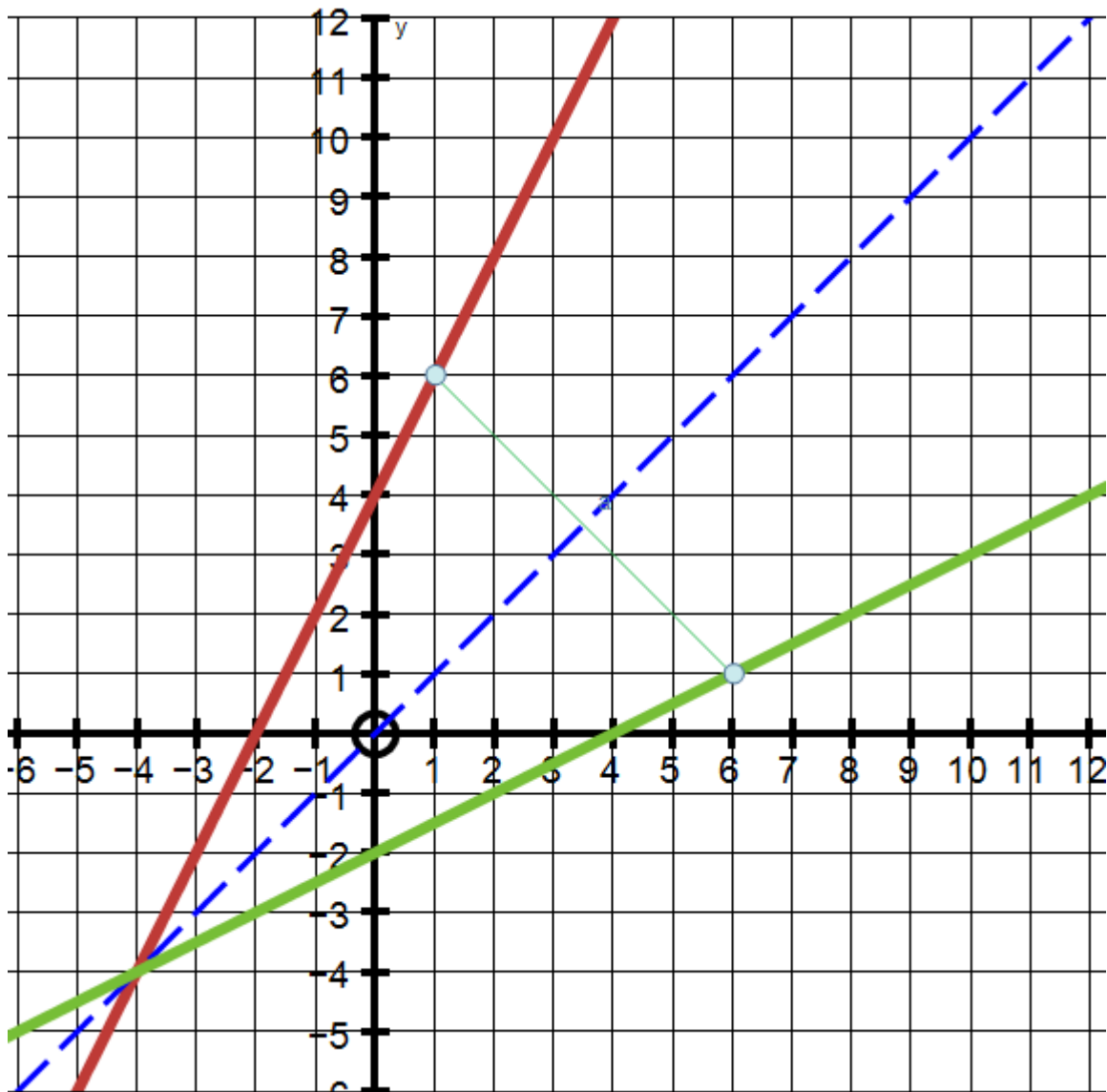


An algebraic method to do this would be to change the equation so that its subject is **x**

$$\begin{aligned} \text{If } y &= 2x + 4 \\ \text{then } y - 4 &= 2x \\ \text{so } x &= \frac{y - 4}{2} \end{aligned}$$

Just testing it.....if  $y = 6$  then  $x = \frac{6-4}{2}$  which does equal  $1$  again!

If we think of  $x = 1, y = 6$  as a point  $(1, 6)$  on a graph then the **inverse point** would be  $(6, 1)$  which is the **reflection of  $(1, 6)$  in the line  $y = x$**



Since these two functions can be thought of as graphs, we usually express each in the form of  $y = f(x)$  and the inverse as  $y = f^{-1}(x)$

In this case  $y = f(x) = 2x + 4$  and  $y = f^{-1}(x) = \frac{x-4}{2}$